

Local Motifs and the Rise of Solidity in Deeply Supercooled Liquids



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Introduction. We investigate the role that Locally Favoured Structures (LFS) play in the emergence of the solid-like behaviour of glassy systems in numerical simulations. To do so, we start from extremely cold configurations ($T \sim 0.97T_g$) and perform a shear experiment testing the zero-temperature limit of a set of rheological properties. We distinguish the more plastic and the more elastic regions and correlate them with the localisation of the LFS.

1. Generating highly structural configurations via importance sampling of trajectories

Locally Favoured Structures (LFS) in supercooled liquids are local particle motifs that are energetically favourable and linked to **transient short range** order.

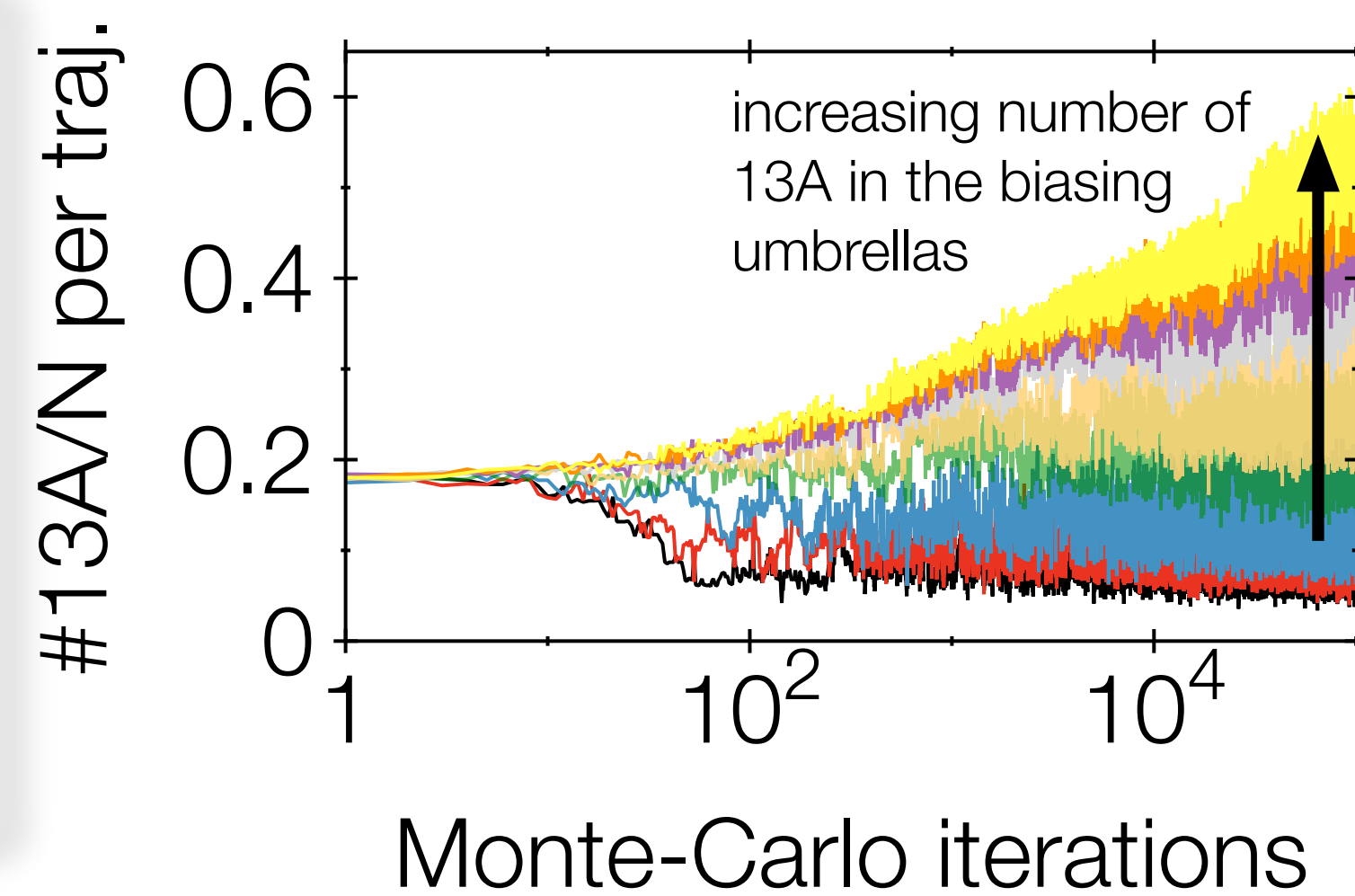


Fig. 1 Sampling trajectories biased according to the time-integrated fraction of icosahedral structures 13A for $N=512$ particles.

We consider a simple binary mixture [1] where icosahedral LFS have been observed. We manage to obtain **high concentrations** of **icosahedra** (13A) via **Transition Path Sampling (TPS)** [2].

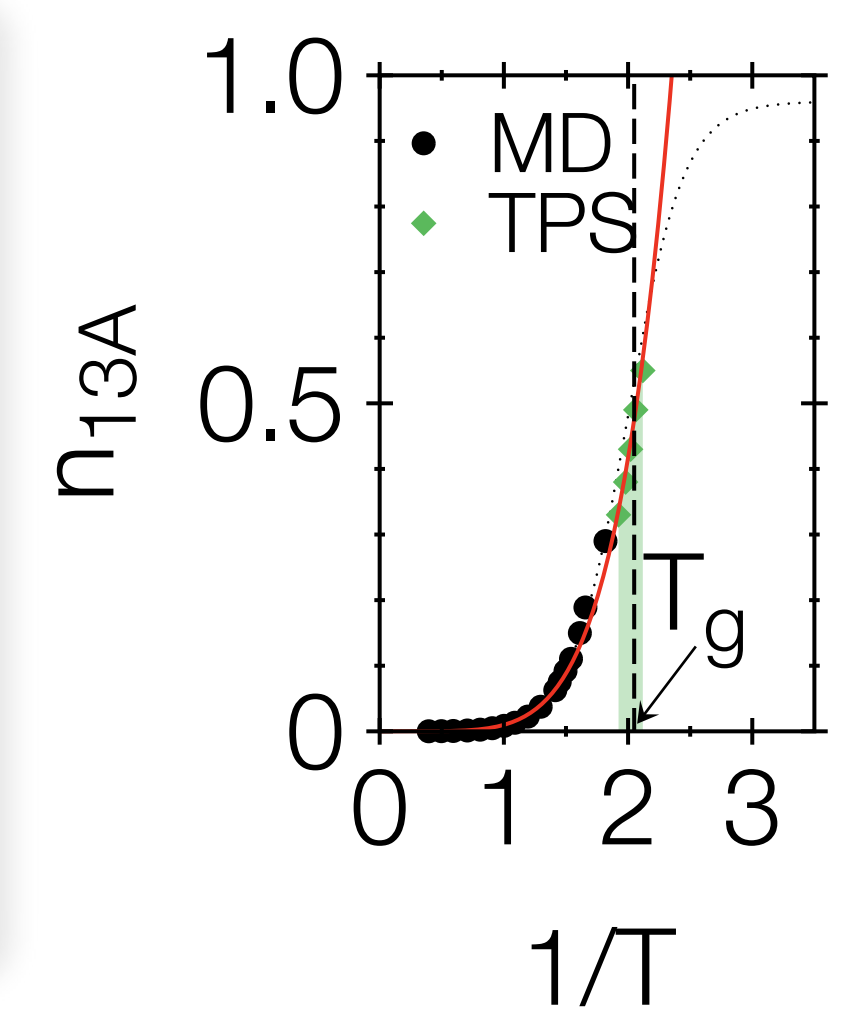


Fig. 2 LFS-rich phases can be interpreted as very cold samples. The corresponding temperature can be extrapolated from the icosahedra growth law determined via standard Molecular Dynamics [2].

2. Probing the mechanical response in the Athermal Quasistatic Limit

The relation between solidity and icosahedral order is probed through a rheological test: the sample is sheared at $T=0$ and performs a succession of **affine deformations** (at constant shear rate) and potential energy minimisations [3].

$$T = 0$$

$$r_{ix} \rightarrow r_{ix} + r_{iy} \delta \gamma$$

$$r_{iy} \rightarrow r_{iy}$$

$$r_{iz} \rightarrow r_{iz}$$

Eq.1 The equations of motion are fully **deterministic** with a constant shear rate $\dot{\gamma}$.

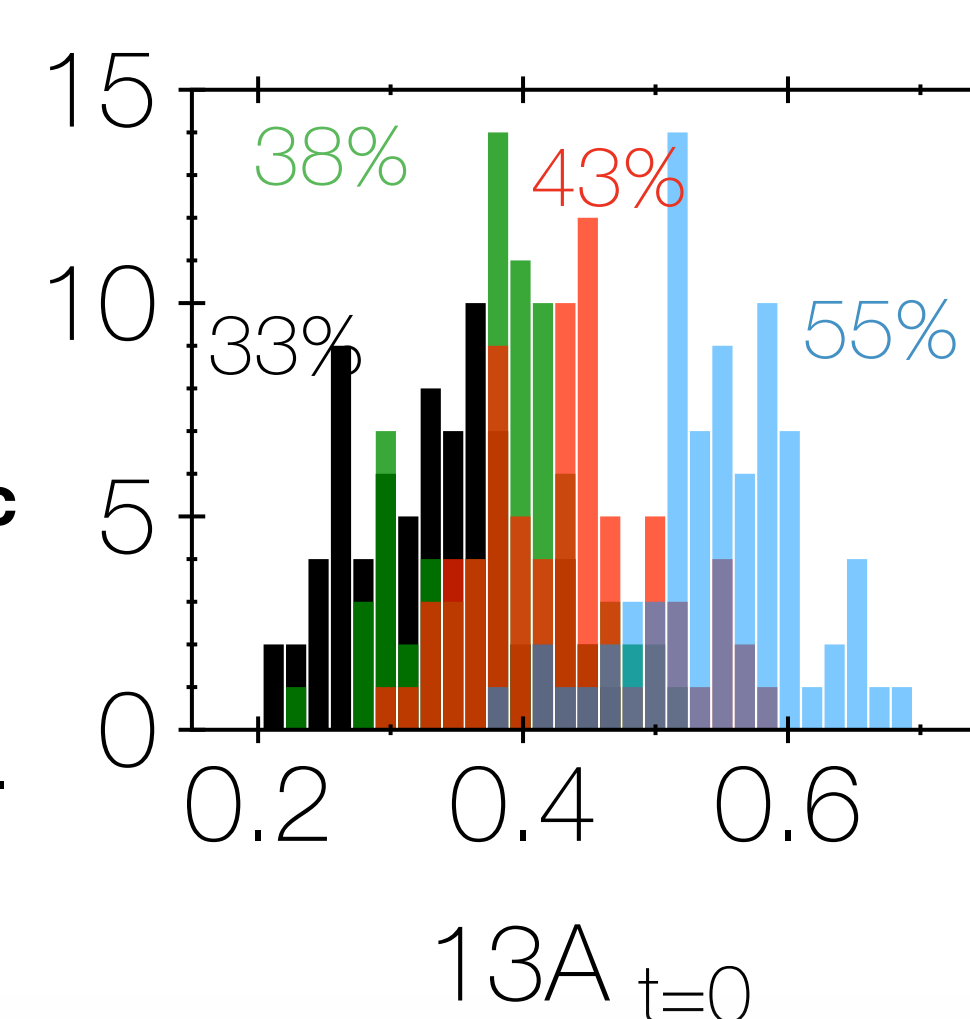


Fig. 3 The TPS umbrellas provide consistent ensembles of configurations characterised by large values of the concentration of icosahedra.

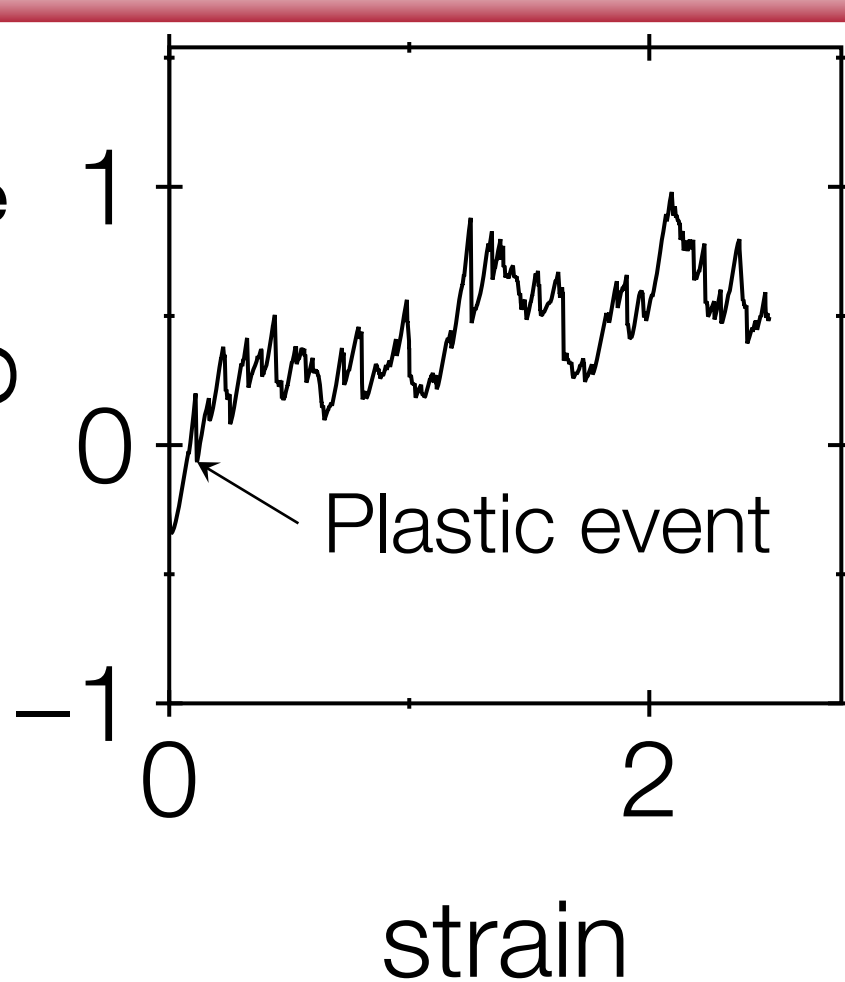


Fig. 4 The potential energy for different values of the strain illustrates the succession of plastic events.

3. More icosahedral structures enhance the yield stress and the elastic modulus

While the energy minimisation initially optimises the fraction of 13A, the shearing protocol leads to a gradual fluidification. This is **strongly dependent** on the initial fraction of icosahedra.

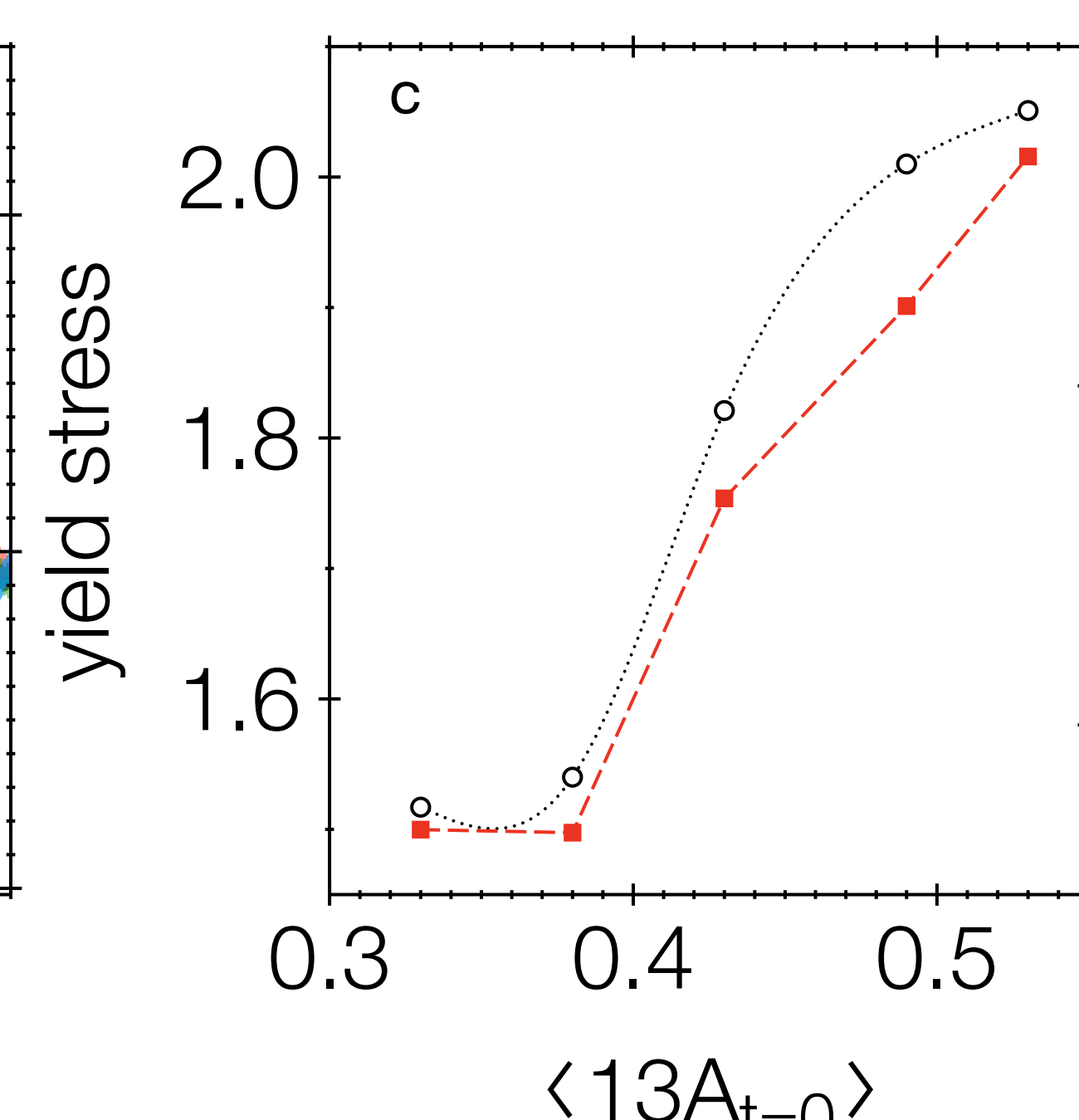
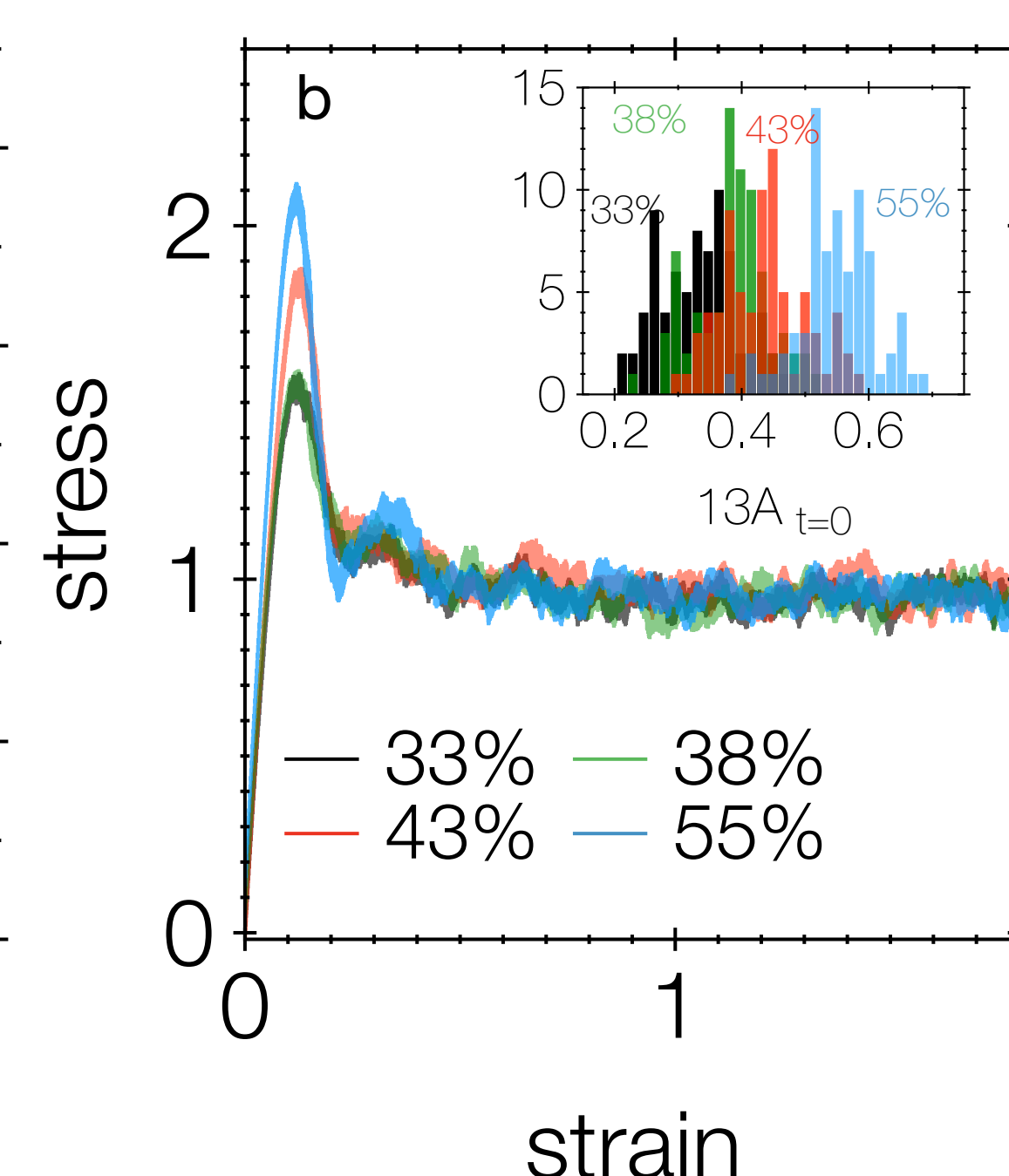
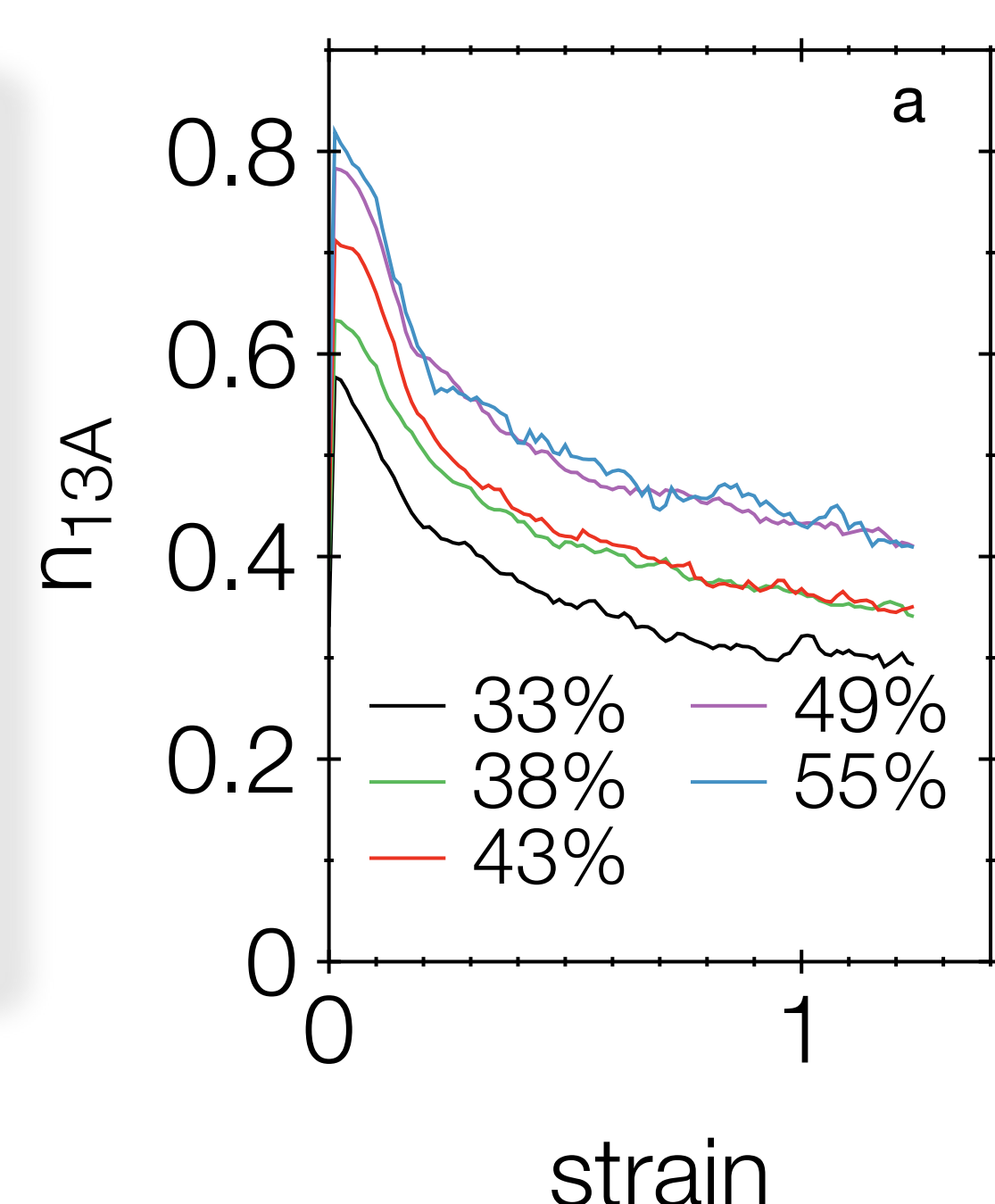


Fig. 5 Fluidification of the the initial configurations: a) decrease of the fraction of icosahedral particles; b) stress-strain curves and c) related measurements of yield stress (stress-peak) and Young's modulus for different initial average concentrations of LFS.

4. The plastic events occur outside the icosahedral clusters

Dynamic information from the **non-affine displacements** [4] and static features from the **mode analysis** [5] anti-correlate with the location of the icosahedral clusters.

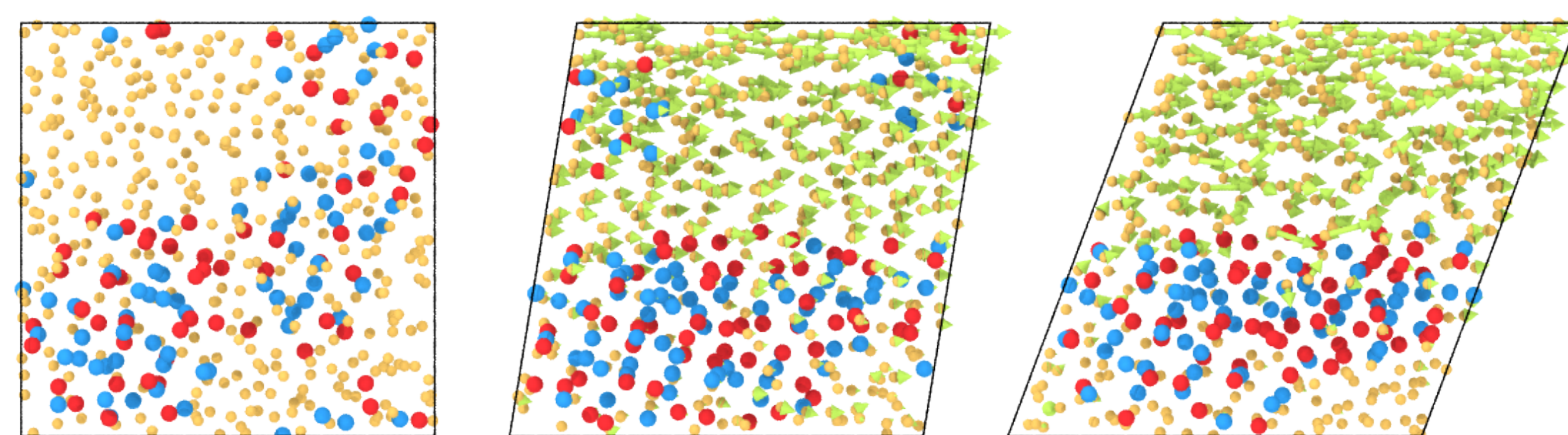


Fig. 8 Displacement field and icosahedral order: shear-banding can be observed, with much larger mobility in the regions not occupied by the LFS structure.

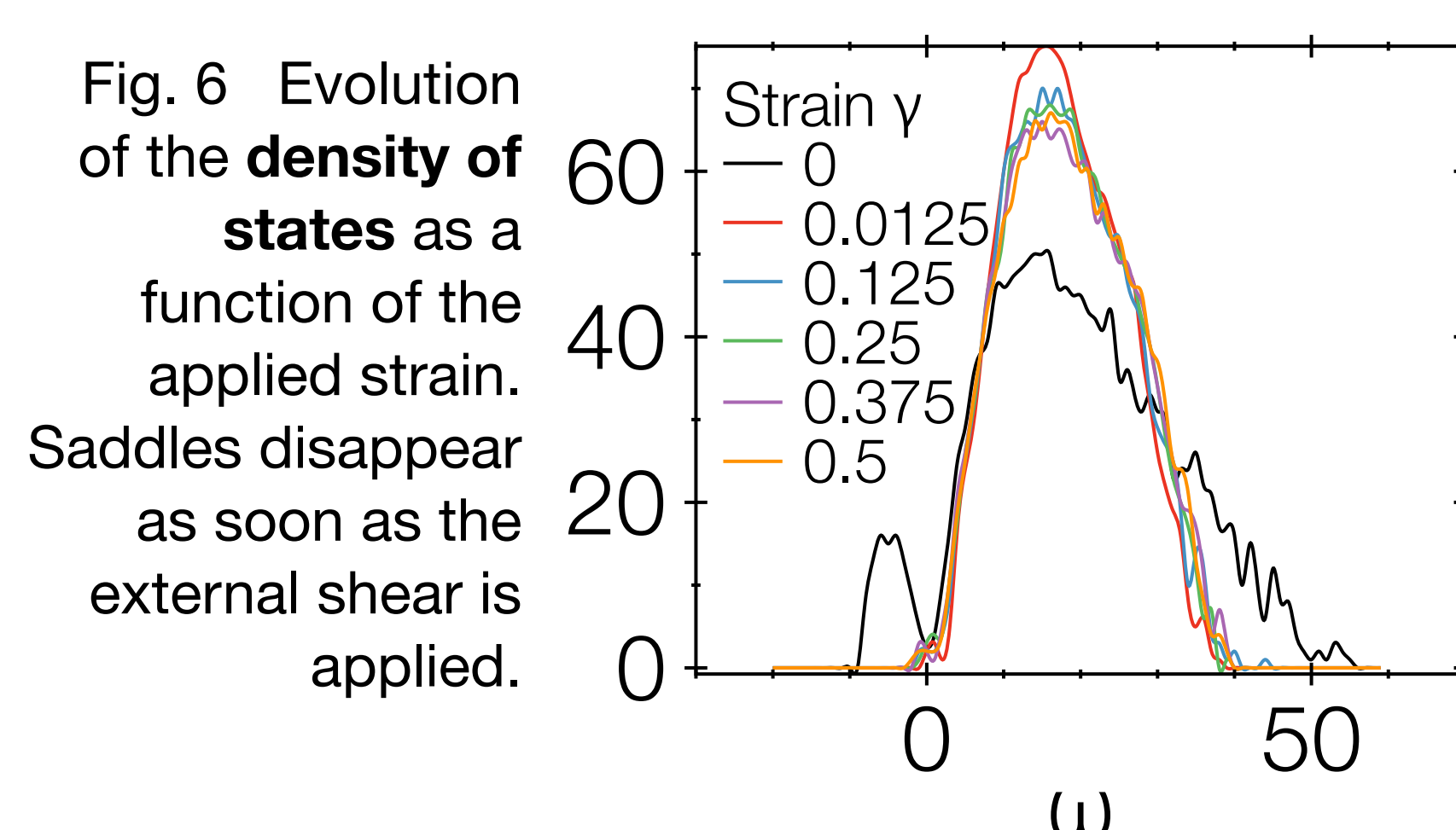
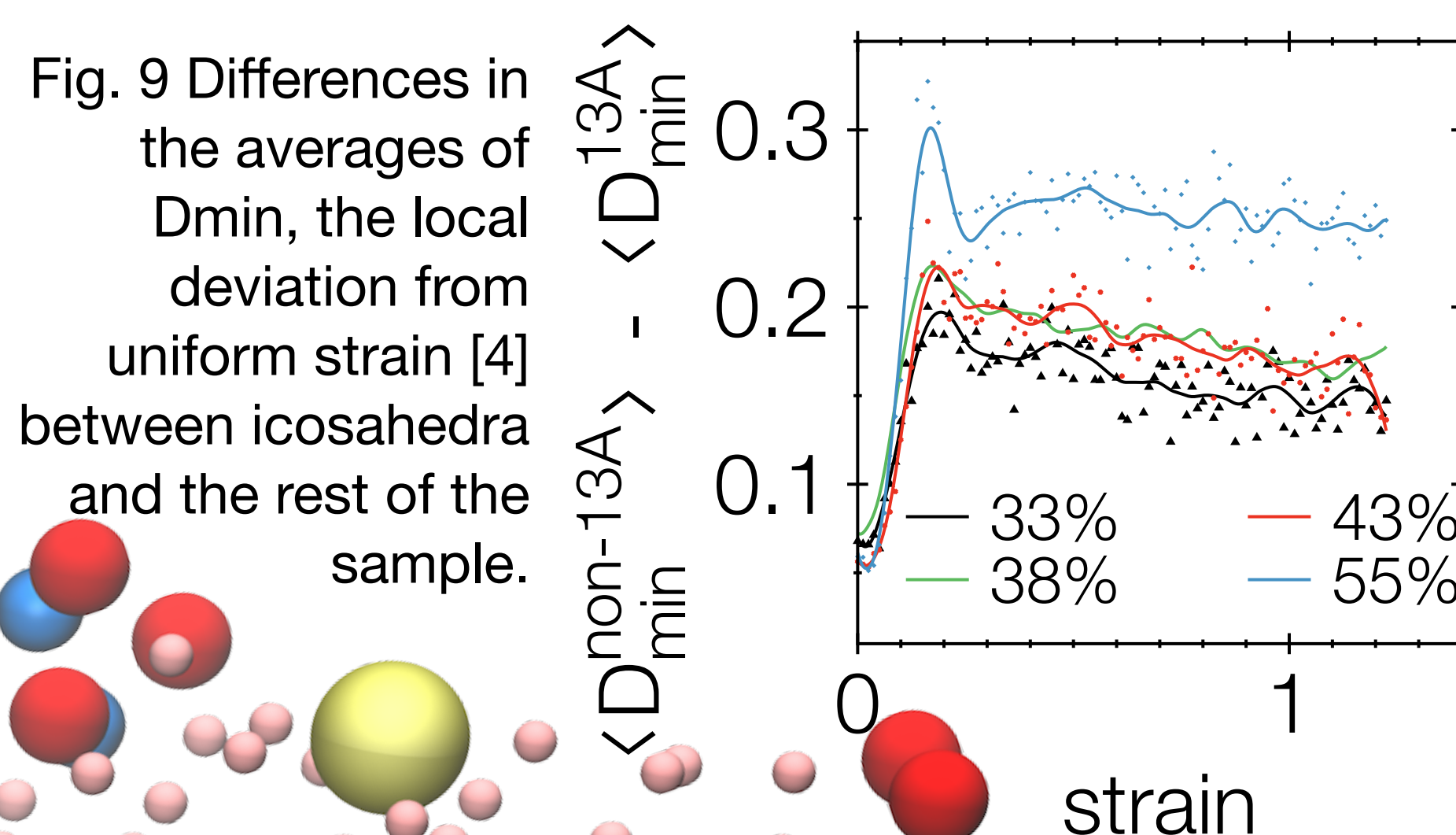
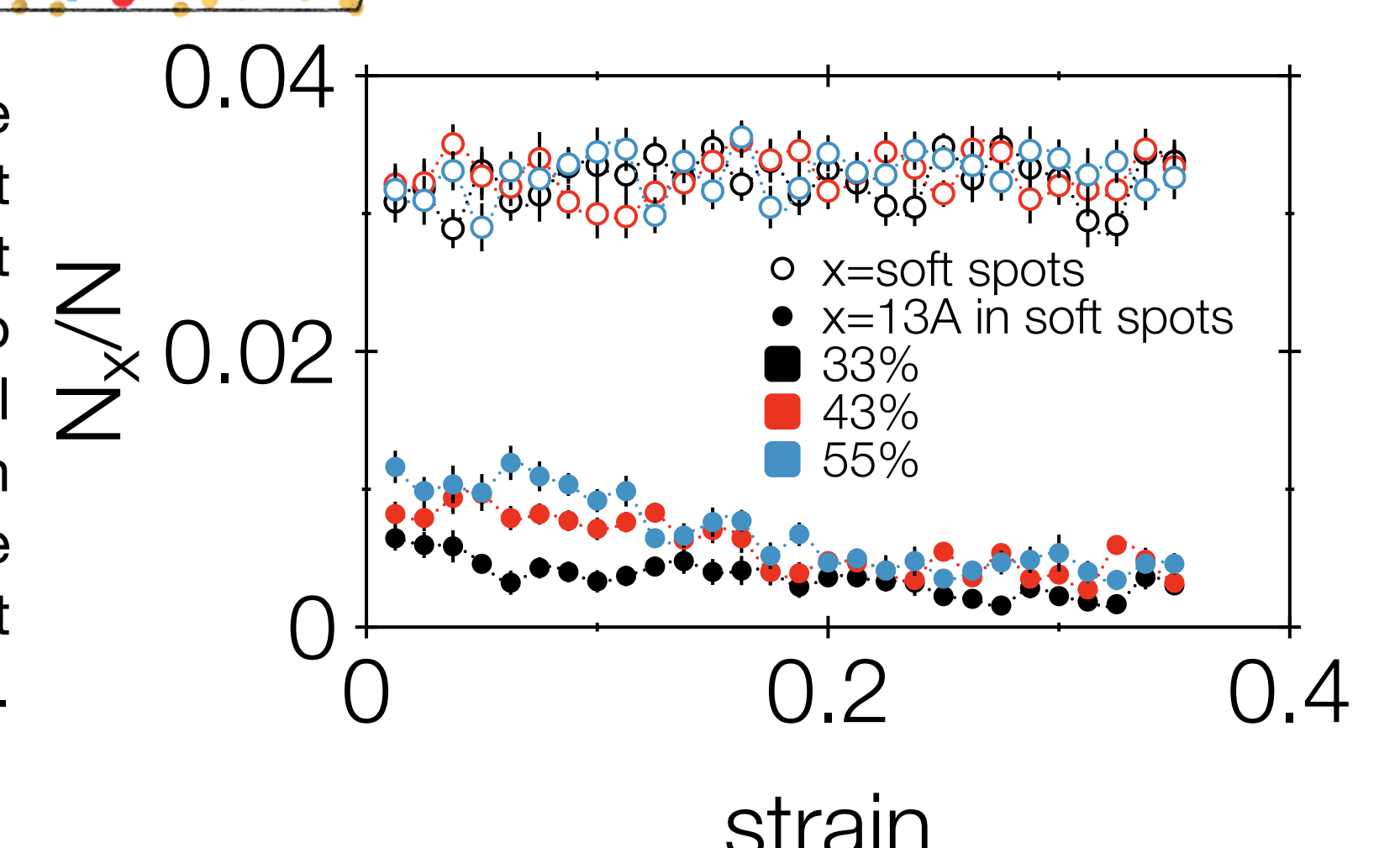


Fig. 7 The large majority of the soft spots is not localised into icosahedral regions, even when these occupy the most of the volume.



Conclusions. Using biased sampling techniques, we obtained **high concentrations** of LFS. These appear to be correlated with the **hardening** of the rheological response. The **localisation** of the LFS is **anti-correlated** with non-affine **displacements** and mobility-triggering **soft-spots**, justifying the interpretation of the icosahedral LFS as the **backbone** of the solid structure of the considered glass former.

References & Acknowledgements

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Fig. 10 The plastic events (determined from the 7 softest modes) are localised outside and in between the icosahedral clusters (in red and blue).